Soundness of Cyclic Proofs in KeY



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KeY Symposium 2023

Daniel Drodt TU Darmstadt











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 - Otherwise proof does not guarantee anything







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Incorrect contracts can be verified

A soundness hole







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 - Otherwise proof does not guarantee anything

One Rule of KeY Is Not Properly Proven Sound

- Incorrect contracts can be verified
 - A soundness hole

We explore the underlying problem and discuss possible solutions.





Rule useMethodContract allows usage of contract ($\psi_{pre}, \psi_{post}, ...$):

 $\Gamma \vdash \mathcal{U}(\psi_{\mathsf{pre}} \land \mathit{wellFormed}(\mathsf{heap}) \land \mathit{paramsInRange}), \Delta$ $\Gamma \vdash \mathcal{UV}(\psi_{\mathsf{post}} \land \mathit{wellFormed}(h) \land ... \land \mathsf{exc} \doteq \mathsf{null} \rightarrow \langle \pi \mathsf{x} = \mathsf{res}; \omega \rangle \varphi), \Delta$

 $\Gamma \vdash \mathcal{U} \left\langle \pi \mathbf{x} = \mathtt{se.m}(\mathbf{a}_1, ..., \mathbf{a}_n); \omega \right\rangle \varphi, \Delta$







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The proof now depends on this contract





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Rule useMethodContractTotal covers recursion:

 $\Gamma \vdash \mathcal{U}(\psi_{\mathsf{pre}} \land wellFormed(\mathsf{heap}) \land paramsInRange \land term \prec \mathsf{mby}), \Delta$ $\Gamma \vdash \mathcal{UV}(\psi_{\mathsf{post}} \land wellFormed(h) \land ... \land \mathsf{exc} \doteq \mathsf{null} \rightarrow \langle \pi \mathsf{x} = \mathsf{res}; \omega \rangle \varphi), \Delta$

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- mby is the termination witness
- Soundness has not been shown
 - Are there theoretical issues?
 - Are there practical limitations or edge cases?





```
/*@ normal_behavior
@ requires num >= 0;
@ measured_by num;
@ ensures \result == 0;
@*/
int m(int num) {
   if (num == 0)
      return 0;
   return m(num - 1);
}
```





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- No additional data needed
- Method m depends only on itself





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- We can verify recursive methods
 - Need termination witness num
- The proof is trivial
- No additional data needed
- Method m depends only on itself
- We model the dependency in a graph:









```
/*@ normal_behavior
  @ requires num >= 0;
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int m1(int num) {
  return num == 0 ? 0 : m2(num-1);
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We can verify m1 and m2 separately





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- We can verify m1 and m2 separately
- Depend on each other





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- Recursion is still bounded by num





```
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```

- We can verify m1 and m2 separately
- Depend on each other
- Recursion is still bounded by num
- We have mutual recursion
- More complex cycle:







```
/*@ normal_behavior
  @ ensures false;
  @*/
void m1() {
  m2();
}
/*@ normal_behavior
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```



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KeY allows verification of m1
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KeY allows verification of m1
 Assumes m2 is correct





```
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- KeY allows verification of m1
 - Assumes m2 is correct
- Will then disallow m2 depending on m1





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- KeY allows verification of m1
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- Will then disallow m2 depending on m1
- We can close KeY and then verify m2
 - KeY loses information about dependencies





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- Might happen accidentally





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When is the rule application sound?



Cyclic Dependencies ...and their soundness







Problem

Cyclic dependencies; units depending on themselves



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Cyclic Dependencies ...and their soundness







Problem

- Cyclic dependencies; units depending on themselves
- Common (theorem provers, package managers, ...)



Cyclic Dependencies ...and their soundness







Problem

- Cyclic dependencies; units depending on themselves
- Common (theorem provers, package managers, ...)

Intuitive Solution

When the cycle (recursion) is bounded, we can allow it



Modeling Proof Dependencies





Contract Dependency Graph



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Contract Dependency Graph

Vertices are pairs of contracts c and methods m







- Vertices are pairs of contracts c and methods m
- Arc from (c_1, m_1) to (c_2, m_2) iff proof for (c_1, m_1) depends on (c_2, m_2)





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Terminating Graphs



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- Strongly connected component is terminating iff
 - It contains no arc or
 - Every contract has termination witness







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- Graph is called terminating iff every strongly connected component is terminating







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Restriction to Rule Applications

Only permit rule applications that result in a terminating Contract Dependency Graph







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Restriction to Rule Applications

Only permit rule applications that result in a terminating Contract Dependency Graph



- Restriction has been proven to ensure soundness
- Not too restrictive







Existing Checks



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Existing Checks

- Similar to the restriction above
- Constructs (a subgraph of) the Contract Dependency Graph







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- Constructs (a subgraph of) the Contract Dependency Graph
- Only considers loaded proofs
- Prone to (accidental) exploits







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- Constructs (a subgraph of) the Contract Dependency Graph
- Only considers loaded proofs
- Prone to (accidental) exploits
- Additional tools exists, e.g., by Wolfram Pfeifer

We need to have persistent information of the global proof state!



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KeY has no notion of "project"

Per-Folder Dependencies

Persistent, but no "project"







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- Persistent, but no "project"
- Dependency information independent of environments and proofs







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Per-Folder Dependencies

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- Dependency information independent of environments and proofs
- When loading folder, parsing Java, creating environment, ...
 - Create dependency repository, load dependency files







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Per-Folder Dependencies

- Persistent, but no "project"
- Dependency information independent of environments and proofs
- When loading folder, parsing Java, creating environment, ...
 - Create dependency repository, load dependency files
- Dependency files contain
 - Dependencies of all proofs of a folder
 - Hashes of contract and method



Dependency Files





```
"/path/to/folder/MyClass1.java" {
}
"/path/to/folder/MyClass2.java" {
    "MyClass2[m1(int)].JML normal_behavior ..."|-217247427|-979473634 {
        "MyClass1[helper()].JML normal..."|102592814|280909408
    }
    "MyClass2[helper()].JML normal_behavior ..."|40138075|-7495401875 {
        "MyClass2[helper()].JML normal_behavior ..."|40138075|-7495401875 {
        "MyClass2[helper()].JML normal_behavior ..."|4010046826|-184653318
    }
}
```





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Shortcomings of Dependency Files



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Shortcomings of Dependency Files

Sensible compromise to change little of KeY's structure





Shortcomings of Dependency Files

- Sensible compromise to change little of KeY's structure
- Additional files are not ideal
- Similar files are necessary/helpful for better proof management





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Introducing KeY Projects



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Introducing KeY Projects

- What approaches and tools exist?
- How to implement this?



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Introducing KeY Projects

- What approaches and tools exist?
- How to implement this?
- Bachelor thesis/project in cooperation with KIT



Conclusion







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- Theoretical foundation for cyclic dependencies \checkmark
 - Provided proper proof of intuitive solution







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 - Provided proper proof of intuitive solution \checkmark
- Added circularity checks for model methods \checkmark







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Overall: Improve correctness of KeY and increase trust in proofs







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- Added circularity checks for model methods
- Proposal for solving soundness issues without undue restrictions \checkmark
- Begin work on improved proof management
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Overall: Improve correctness of KeY and increase trust in proofs

Thank you for your attention!

